



Splitting shopping and delivery requests in an on-demand personal shopper service

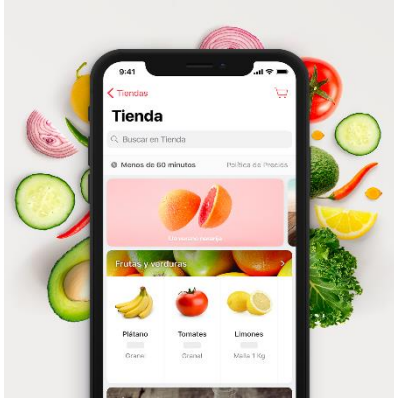
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- ❖ Motivation: online personal shopper services
- ❖ Our strategy
- ❖ Solution method
- ❖ Experiments
- ❖ Takeaways

Motivation: online personal shopper services



PS services are intermediaries who:

1. **receive** online customer requests (a shopping list),
2. **shop and pick-up** items available at local retailer stores,
3. **and deliver** these to the customer within a short deadline (e.g. 2 hours).

- Idea:

convenience of online shopping + product availability at stores.

Increasingly popular for grocery delivery

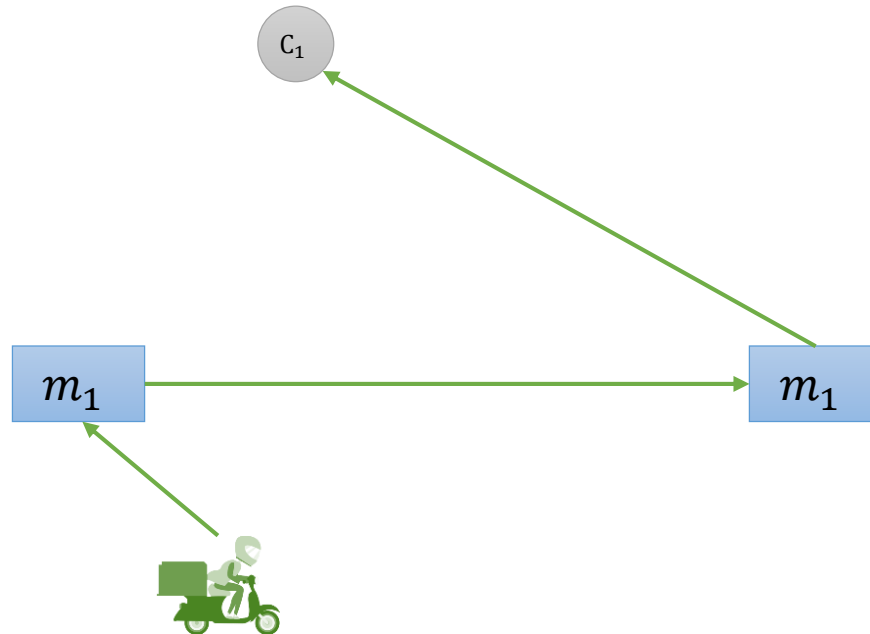


- Biggest PS service provider: **Instacart** (US)
 - ≈\$8 billion market value, 300 retailers partners, operates in 50 US states
- **Postmates** (US), **Deliv** (US), **Rappi** (Colombia), **Cornershop** (Chile - México), **Glovo** (Spain),
- Similarity to meal delivery services (**Grubhub**, **UberEats**, **Foodora**)

PS service business model

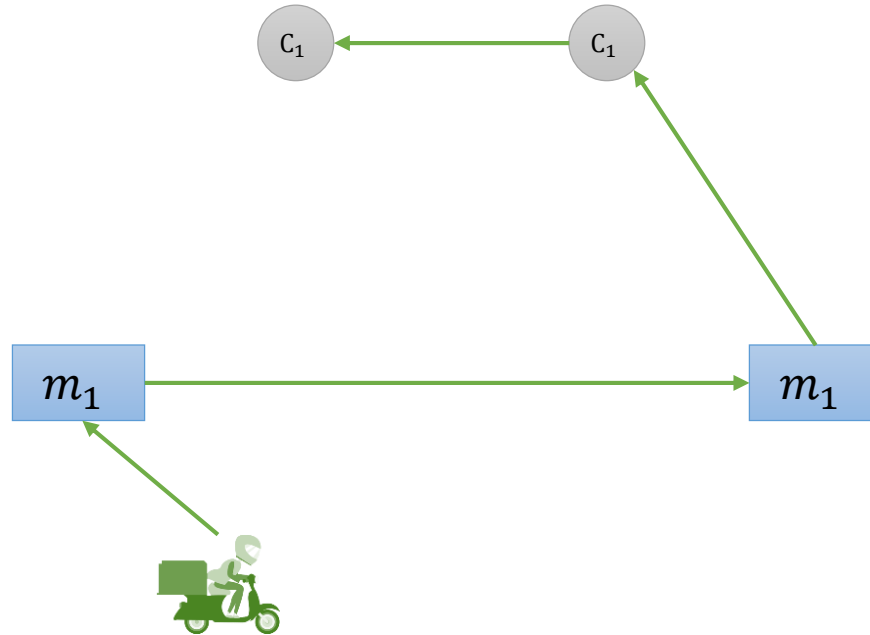
- A PS service is a **store aggregator**:
 - Offers products of affiliated Brick & Mortar stores.
 - Google Shopping: 50 merchants: Costco, Target, Walgreens...
 - Asset-light business (no inventory).
- Also, it is a **logistics service provider**:
 - Online platform accepts customers' shopping requests.
 - Automatic dispatcher assigns accepted requests shoppers.
 - **Shopper**: Shops and delivers items to customers.

Simple strategy: One request per shopper at a time



Customer c_1 orders from stores m_1 and m_2 .

An improvement: consolidate if possible

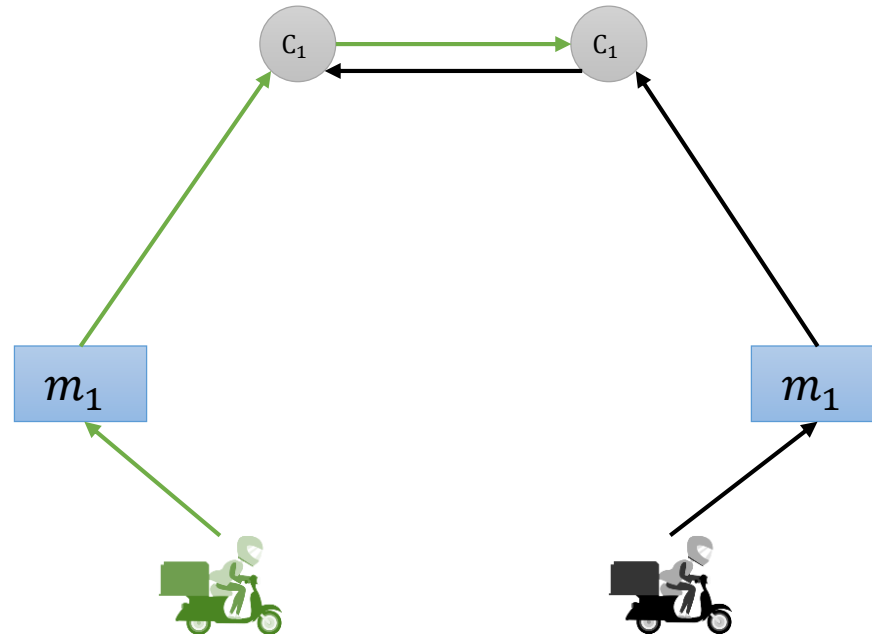


Customers c_1 and c_2 order from stores m_1 and m_2 .

But: tight delivery deadlines \rightarrow limited consolidation options.

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Our strategy: split requests & deliver in parallel



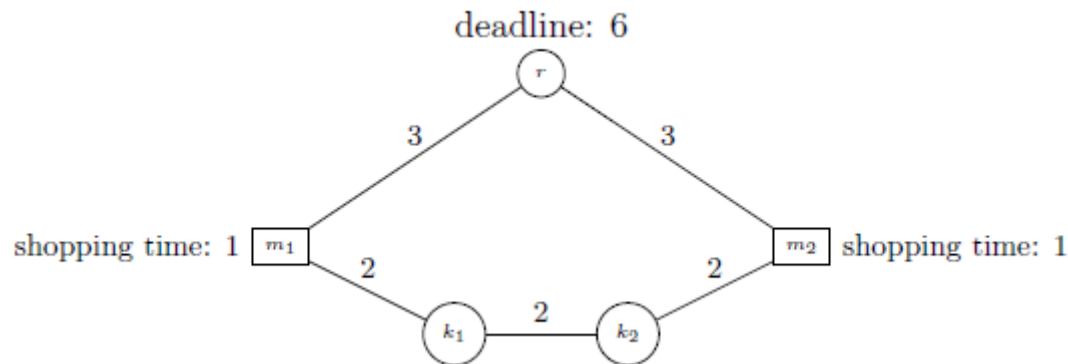
- We study splitting the service of requests involving shopping at multiple stores into separate **tasks** served by different shoppers.

Less granularity & more flexibility

Dividing requests into smaller task may create:

Packing benefits: increased fleet time utilization & capacity.

- Particularly relevant when delivery deadlines are tight.

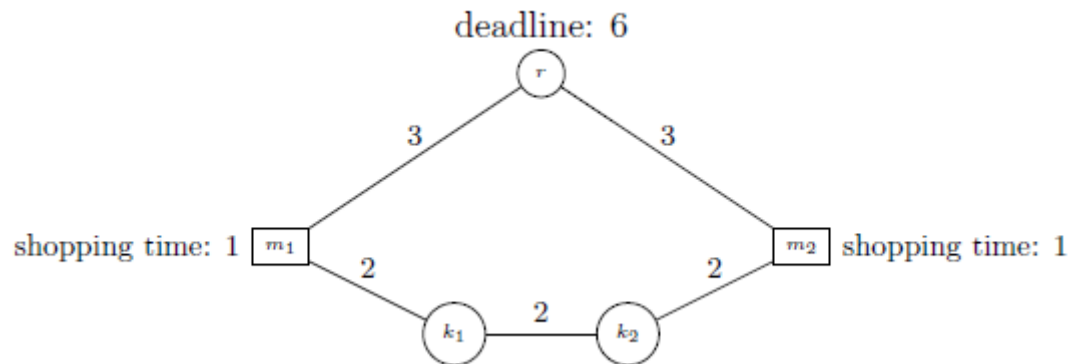


- An on-time service is infeasible without splitting ($t \geq 13$).
- If the request is split into two tasks, then two shoppers can deliver by $t = 6$.

Less granularity & more flexibility

Dividing requests into smaller task may create:

Routing benefits: a larger set of routing options may require less travel time.



- Single shopper total travel 11 time units
- Two shoppers total travel 10 time units

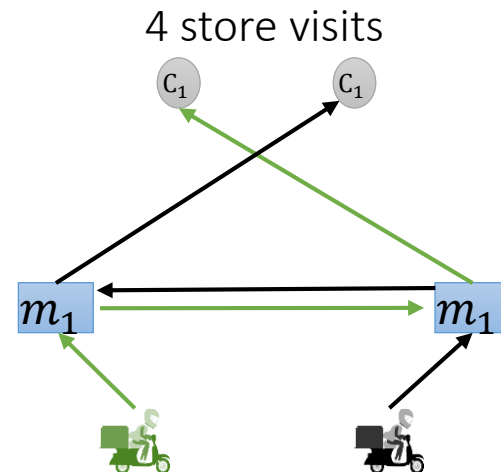
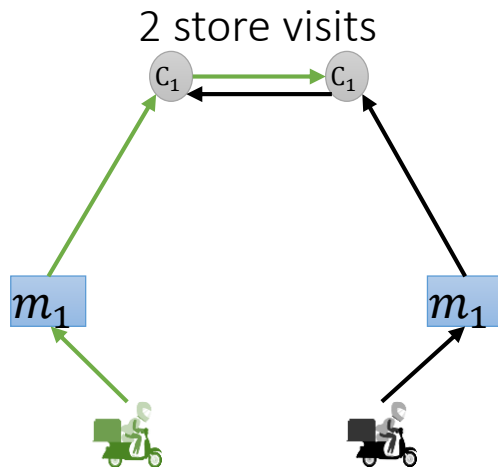
Less granularity & more flexibility

Dividing requests into smaller task may create:

Shopping benefits: save fixed shopping times by consolidating in one shopper multiple tasks originated in a common store.

$$\text{Shopping time} = f + \sum_{s \in S} v_s$$

- Variable shopping time is unavoidable, but we could save store visits (parking, queuing, walking to store).



Related Literature

- **Pick-up and delivery:** Salvendy and Sol, (1995), but dynamic & multiple pick-ups per delivery.
- **Split delivery routing problem:** Archetti et al. (2008), Nowak et al. (2009): similar flexibility principle, different problem.
- **Same-day delivery:** Arslan et al. (2019), Klapp et al. (2018), Voccia et al. (2017), Ulmer (2018): same-day delivery with multiple pickup locations.
- **Meal delivery problem:** Reyes et al. (2018); Ulmer et al. (2017); Yildiz and Savelsbergh (2017); Steever et al. (2019).
 - Relatively more constrained, different objectives

Problem Statemet

- A service period T in which customers place requests.
- Set of partner retailer stores M .
- Dynamically arriving customer requests $r \in \{1, \dots, n_R\}$ with:
 - Required delivery location
 - Shopping list from one or more stores in M
 - Order placement time e_r
- System-wide delivery deadline L . Latest delivery time $e_r + L$
- Fleet of shoppers K

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Tasks and graph representation

- A customer's shopping list is a collection \mathcal{S}_r of tasks with common delivery location.
- A **task** is a pair of shopping s^+ and delivery s^- nodes.
- **Task based network representation:**
 - can model fixed and task-dependent store times as arc costs.

Location-based representation



Task-based representation

Model

- Assume event-based sequential decisions triggered by request arrivals with no prior future knowledge (pure online problem).
- State at decision time t :
 - set of active tasks S_t , *i.e.* accepted but not yet served,
 - shopper status: location, earliest departure and load info,
 - delivery plan: a pick-up and delivery trip per shopper.
- Decisions at time t :
 - accept or not: we accept when it is feasible,
 - Update and execute delivery plan until next decision time.
- Objective: Maximize number of requests served on-time.

A rolling horizon framework

Our solution:

- solve **routing problem (PsDPd)** before each acceptance decision to identify a feasible plan covering new and active tasks.
- If such a plan is found, then accept and update plan.
- **PsDPd**: pick-up and delivery routing problem, but
 - Multiple pick-ups per request and split delivery,
 - service deadlines,
 - considers current state of shoppers & en-route assignments.
 - Minimize total shopping and travel time.

PsDPd solution approach #1: Exact approach

1. Partition all active tasks among the shoppers
2. Test feasibility with DP labeling algorithm similar to Tilk and...
 - Hamiltonian path problem with deadlines
 - Algorithm...
 - Lower bound.
 - **Specific label domination** rules acknowledging that distances between pick-ups in a common store have no path dependency.



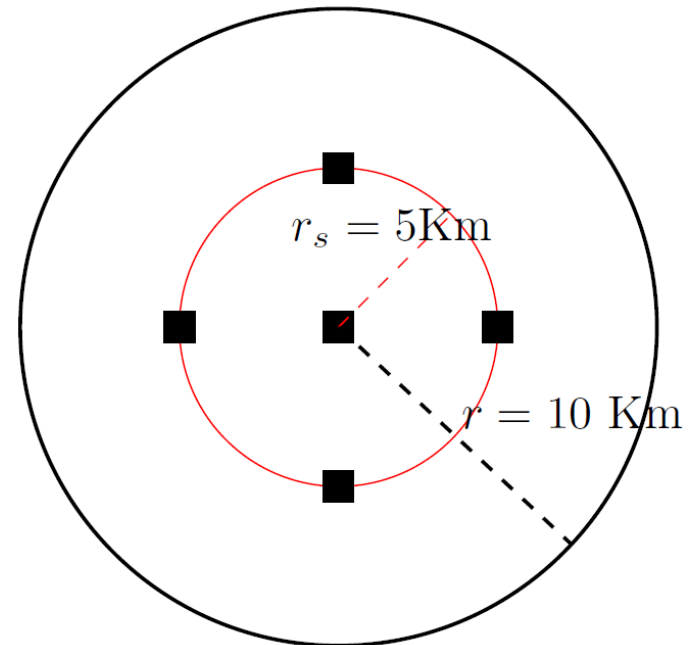
PsDPd solution approach #2: PlanMaker heuristic

- Split new request into tasks.
- Sequential cheapest insertion by task.
- Adaptive large neighborhood search (ALNS):
 - Removal operators: partial destruction of solution by removing certain tasks.
 - Repair operators: reinsert the removed tasks.
- Choose repair operators according to dynamically updated weights based on success.

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Computational Experiments

- 10km radius area, five stores located within a 5Km radius.
- Uniformly distributed customers over space and time.
- 10 hours service period.
- Each request demands shopping from three randomly chosen stores
- Five shoppers, max capacity 10 tasks.



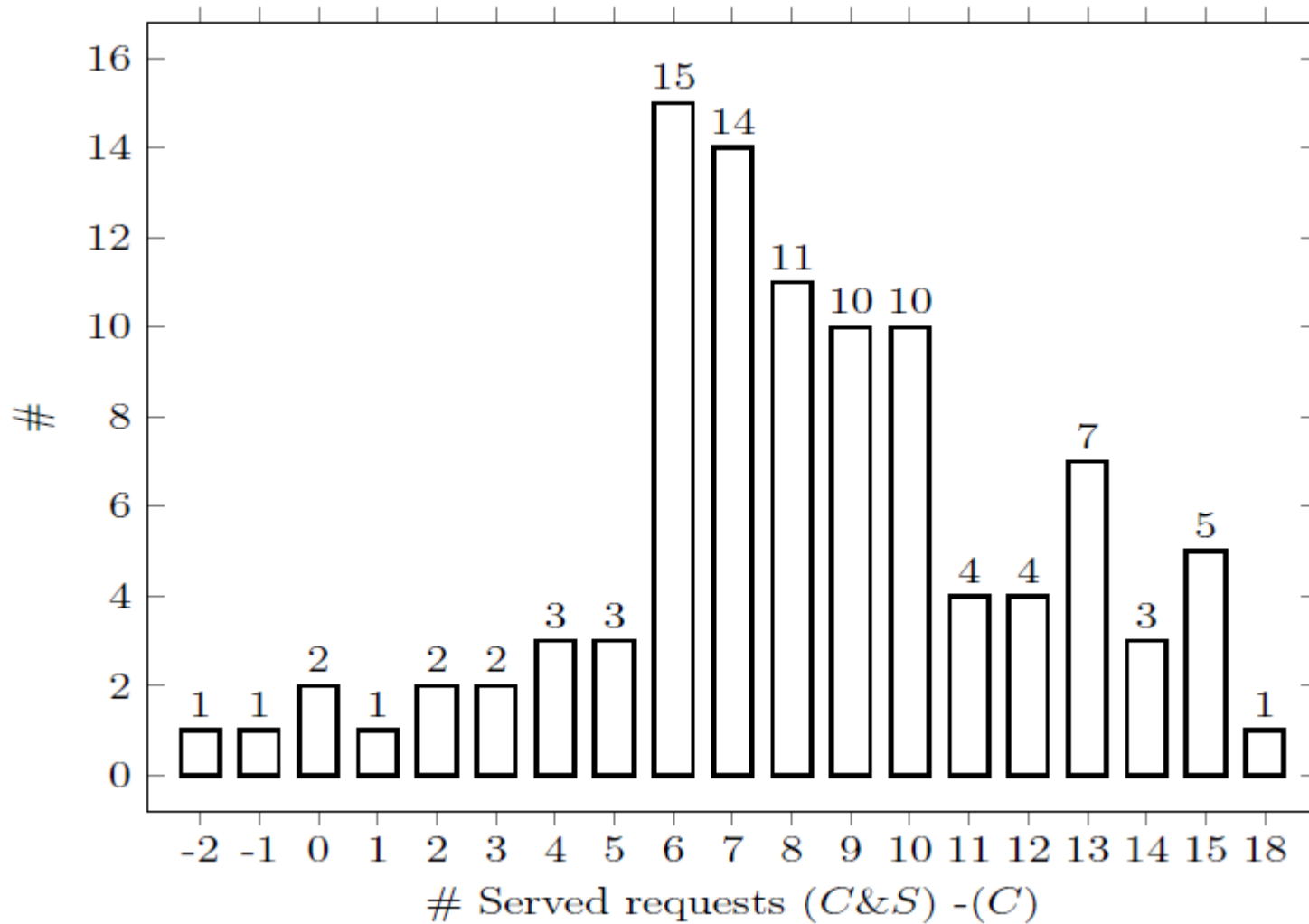
Tested operational policies

- **One by one (1b1):** Each shopper serves one single customer request at a time.
- **Consolidation (C):** A shopper can simultaneously serve multiple requests, but all tasks of a single request are served by one single shopper.
- **Consolidation & Splitting (C&S):** Requests can be split into different tasks that can be served by multiple shoppers in parallel. Also, shoppers can simultaneously serve tasks of multiple requests.

Base Case Results ($L = 90\text{min}$)

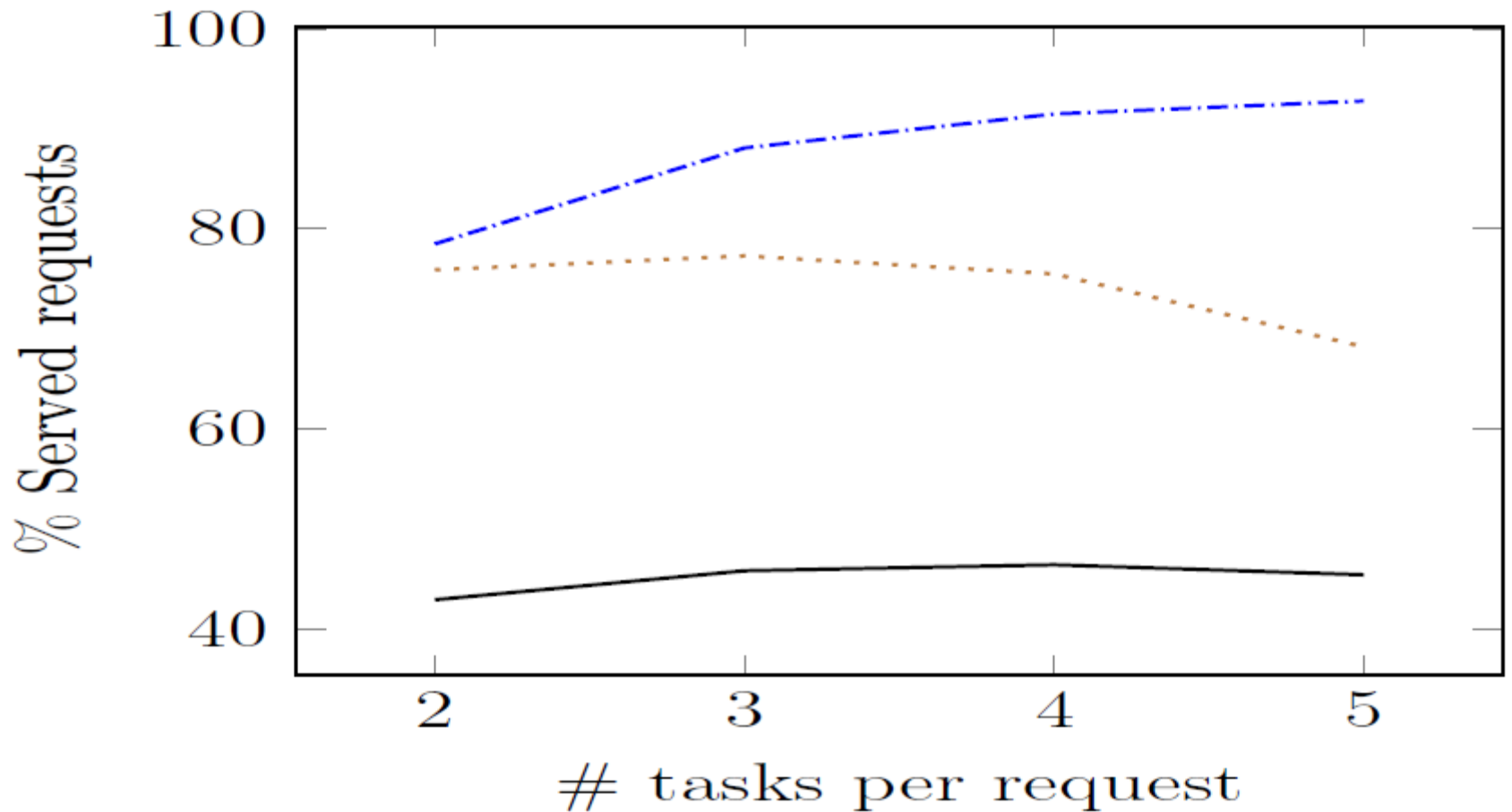
| | $1b1$ | C | $C\&S$ |
|------------------------------|-------|------|--------|
| Served requests (%) | 45.8 | 77.3 | 88.1 |
| Request split. (%) | 0 | 0 | 69.2 |
| Delivery interval (min.) | 0 | 0 | 23.6 |
| Time per req (min.). | 51.2 | 28.9 | 25.1 |
| Shopping time per req (min.) | 30.0 | 15.0 | 10.3 |
| Travel time per req (min.). | 21.2 | 13.9 | 14.8 |
| # locations visited per req. | 4.0 | 2.3 | 2.7 |
| CtD (min.) | 77.1 | 78.2 | 77.3 |

Base Case Results ($L = 90\text{min}$)



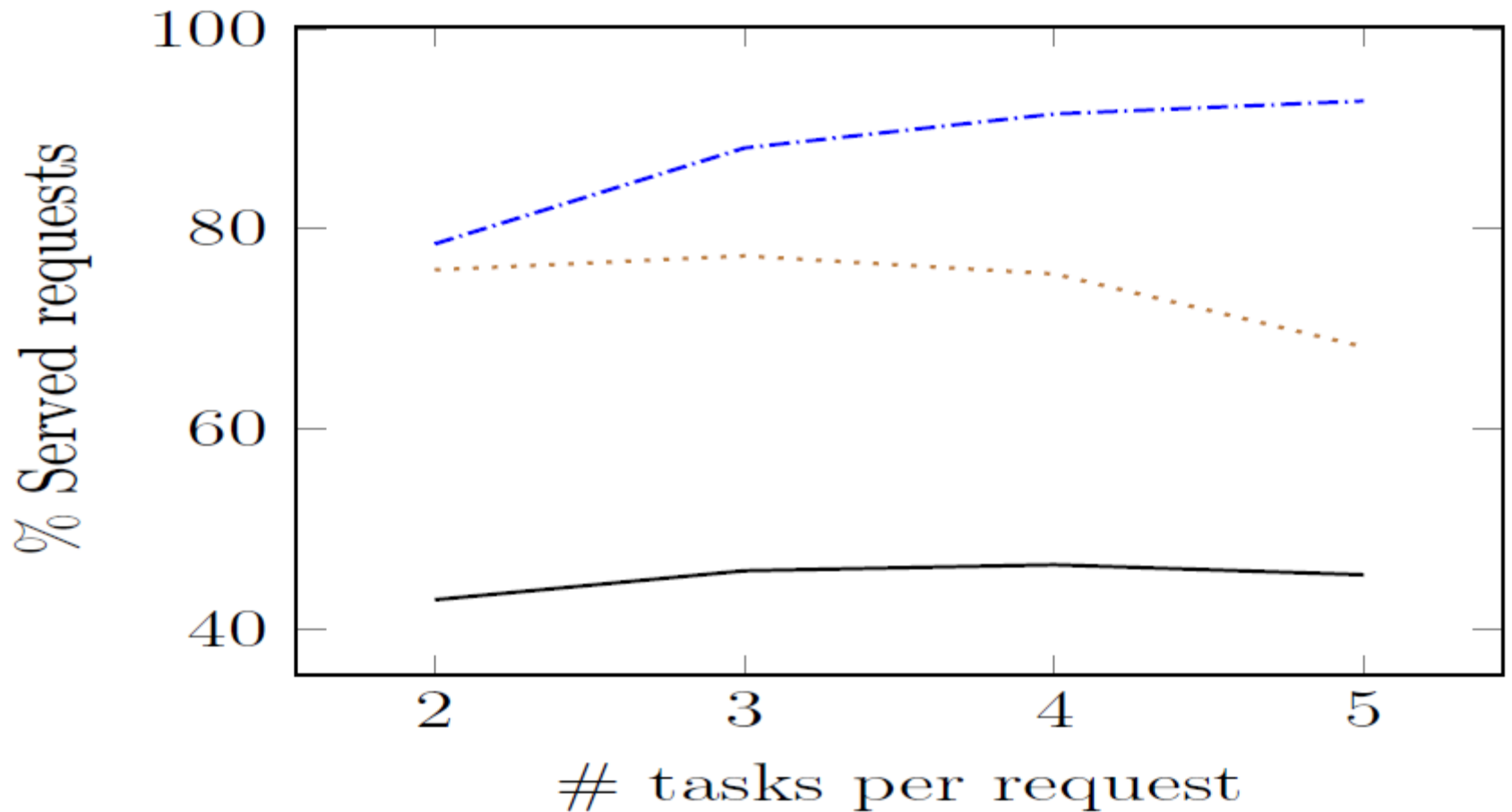
Sensitivity: # tasks per request

(a) Served requests



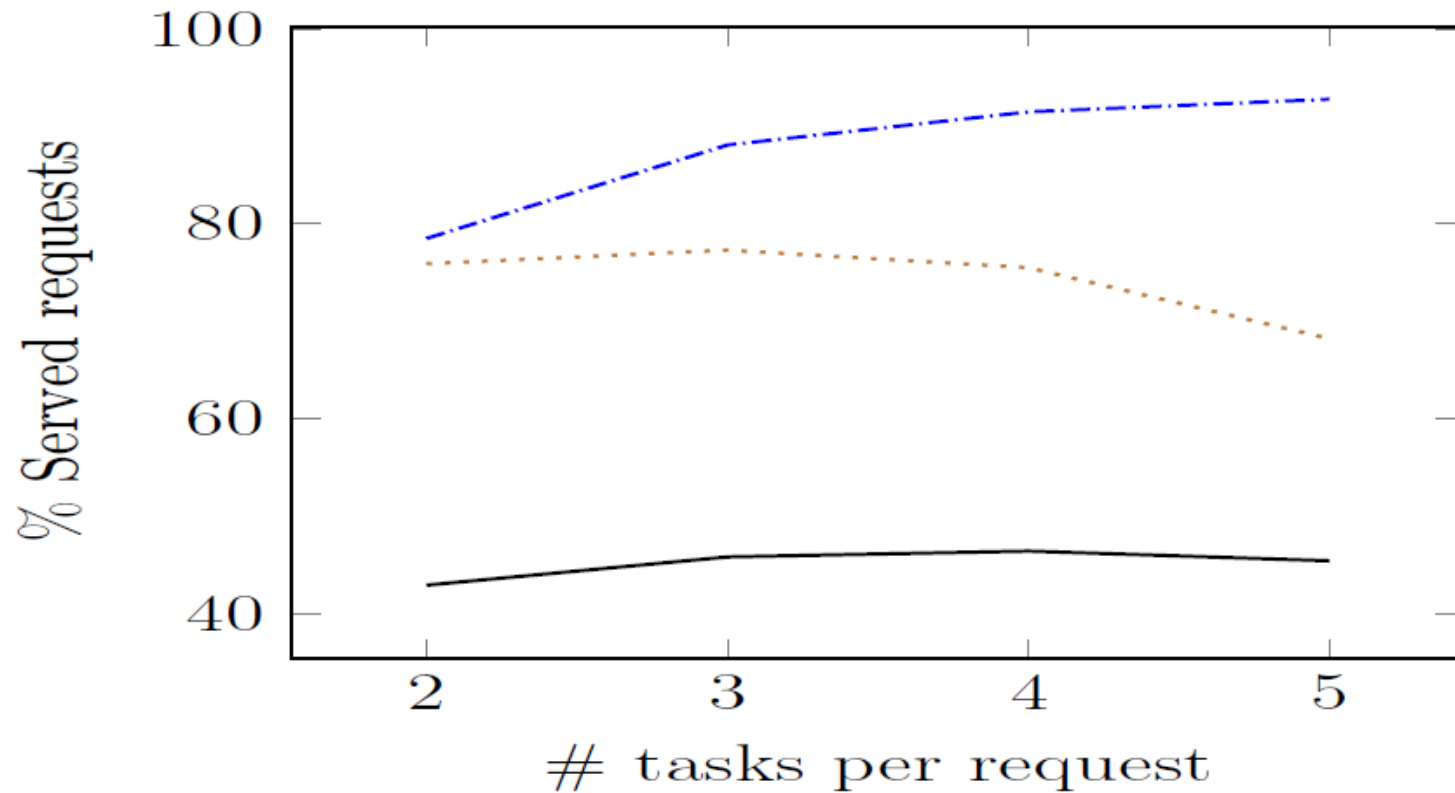
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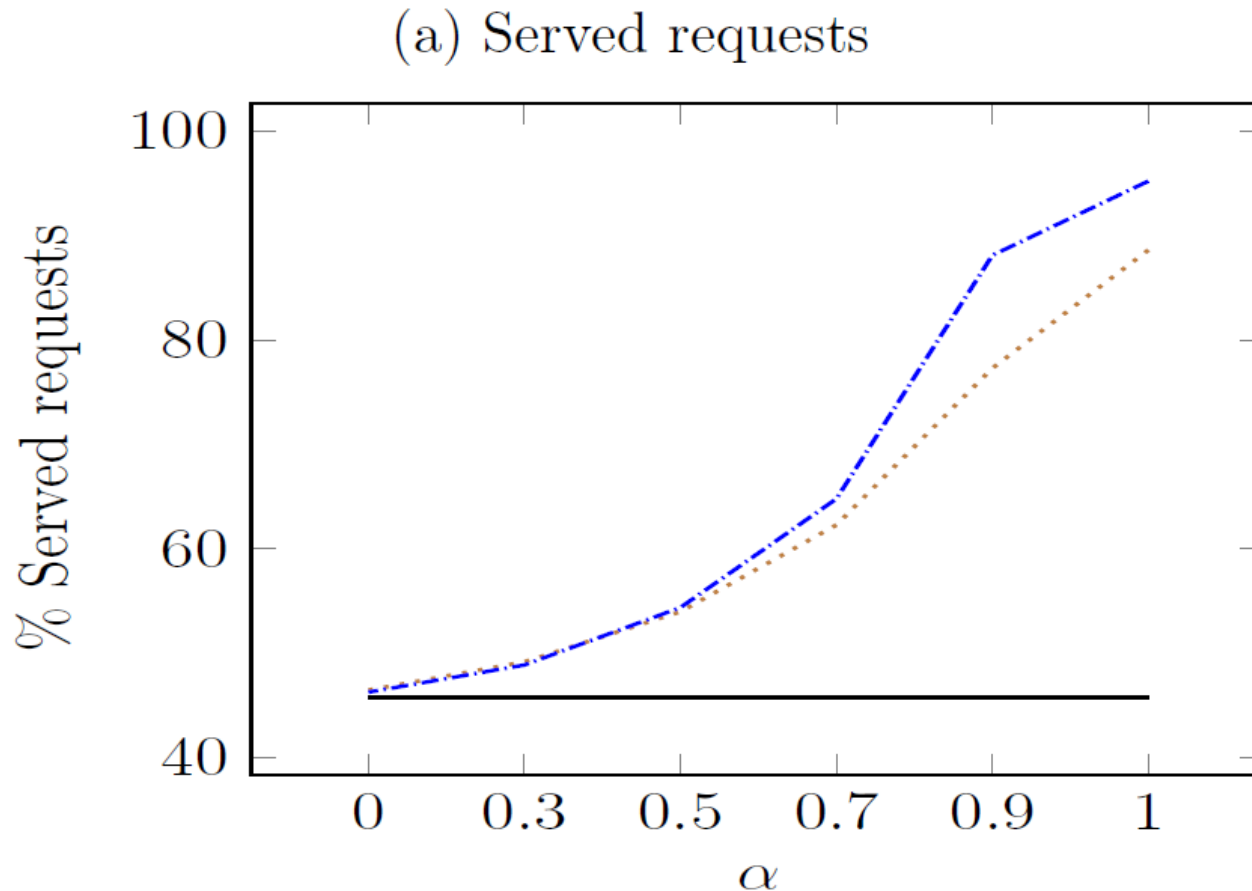
— *lb1*

..... *C*

-.-.- *C&S*

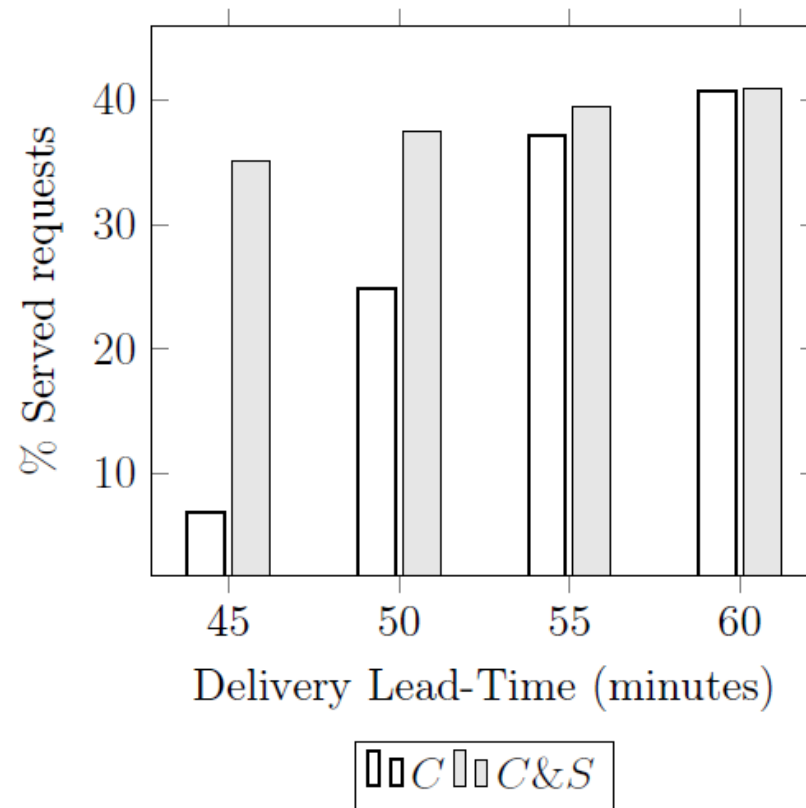
Sensitivity: shopping economies at stores (α)

- $\alpha = 0$: shopping time proportional to tasks collected.
- $\alpha = 1$: fixed shopping time per store visit.



Sensitivity: delivery deadline (and packing benefits)

Figure 7: Packing Benefits of Request Split, $\alpha = 0$, 80 Requests, 3 Shoppers

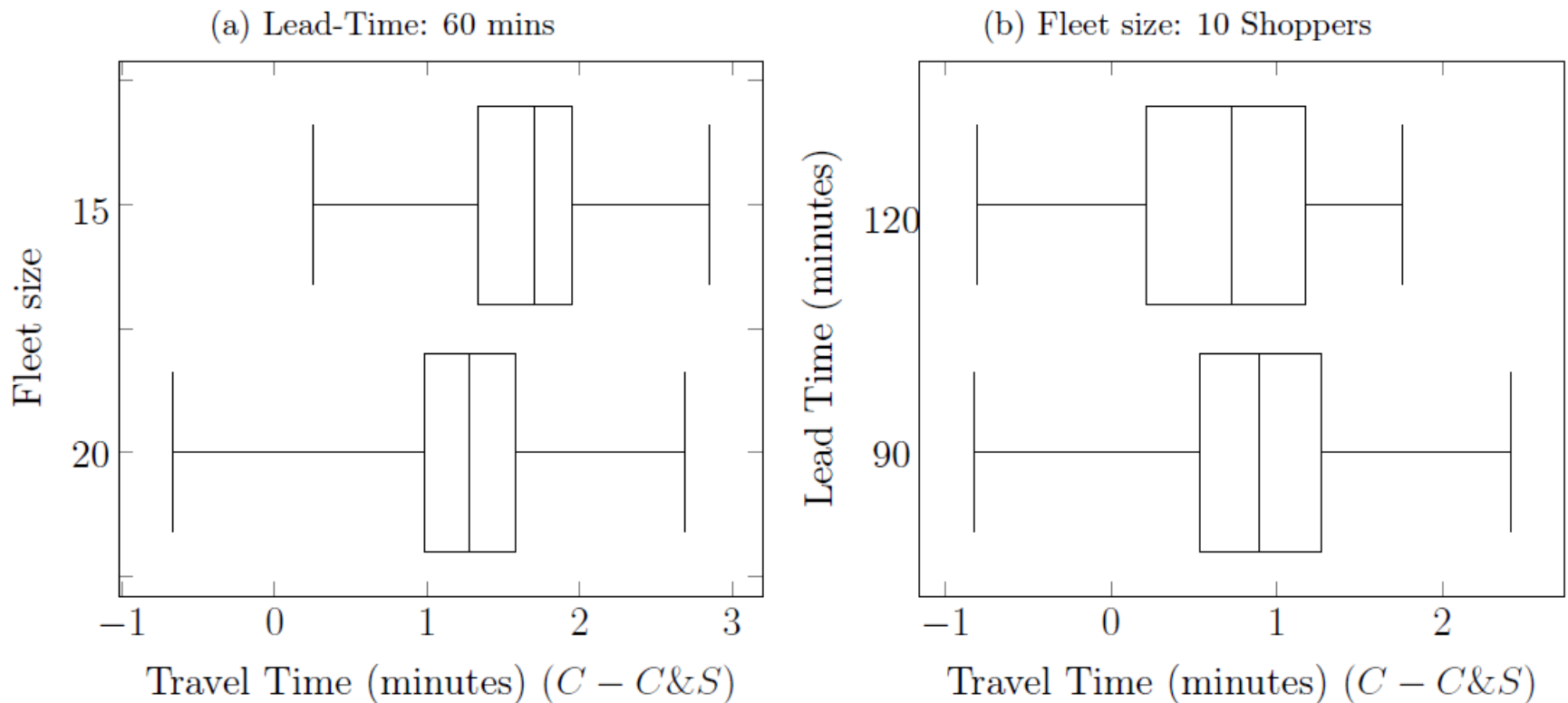


- We focus specifically on packing and routing benefits (no shopping economies)

Routing Benefits

- We focus specifically on routing benefits (no shopping economies, enough capacity to serve 100%)

Figure 8: Routing Benefits of Request Splits When No Packing Benefits: $\alpha = 0$, **80 Requests**



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Key Takeaways

- Request splits increase the percentage of served requests.
- On average customers also receive faster delivery.
- Benefit mostly obtained due to an increased shopper utilization, reduced shopping times, and cheaper routing options available.
- Benefits of splitting increase for relatively more time constrained systems with stronger shopping economies.

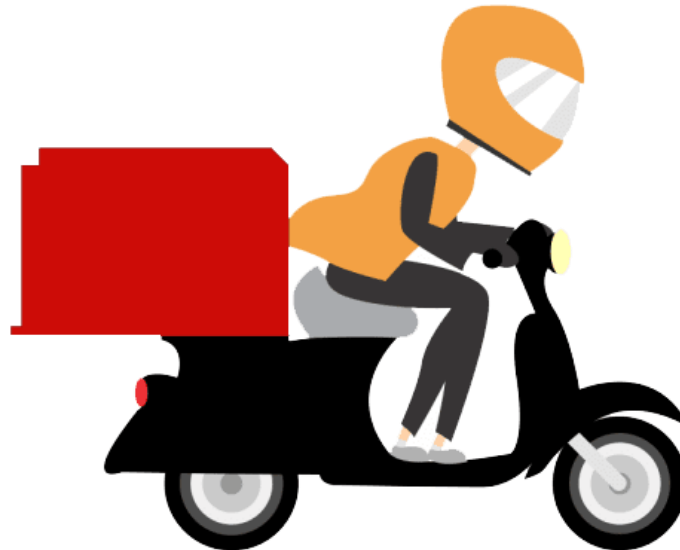
Future Work:

- Probabilistic information about the future and proactivity.
- Splits and transfers?
- Separating shopping and delivery?

Questions?

“Splitting Shopping and Delivery Tasks in an On-Demand Personal Shopper Service”

Draft available at <https://dx.doi.org/10.2139/ssrn.3428912>



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PlanMaker validation in small instances:

| n_s | Av. Opt. gap (%) | # Optimal | Δ Feasibility |
|-------|------------------|-----------|----------------------|
| 8 | 1.3 | 4/5 | 0 |
| 9 | 1.5 | 4/5 | 0 |
| 10 | 4.0 | 3/5 | 0 |
| 11 | 0.8 | 4/5 | 0 |
| 12 | 2.1 | 3/5 | 0 |
| 13 | 2.8 | 4/5 | 0 |
| 14 | 3.7 | 1/5 | 0 |
| 15 | 3.1 ¹ | 0/5 | 1 |

Para responder a su pregunta:

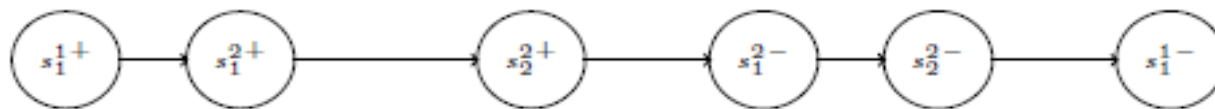
Table 4: Empirical Distribution of click-to-door time and delivery Interval for the *C&S* policy.

| | click to door (<i>CtD</i>) | | | delivery interval |
|---------|------------------------------|-------|------|----------------------|
| | non-split | split | All | |
| minimum | 15.0 | 37.8 | 15.0 | 0.01 |
| Q1 | 71.4 | 72.9 | 71.7 | 7.3 |
| Q2 | 81.7 | 82.2 | 81.8 | 18.3 |
| Q3 | 87.2 | 86.8 | 87.3 | 34.9 |
| maximum | 89.9 | 89.9 | 89.9 | 85.7 |
| average | 77.2 | 78.1 | 77.3 | 23.6 |

Para responder a su pregunta:

$$c_{ij} := \mathbb{1}_{\binom{\mathbf{L}}{i \neq j}} t_{ij} + \mathbb{1}_{(j \in S^+)} \left(c_j^p + \mathbb{1}_{\binom{\mathbf{L}}{i \neq j}} c_j^f \right),$$

Location-based representation



Task-based representation